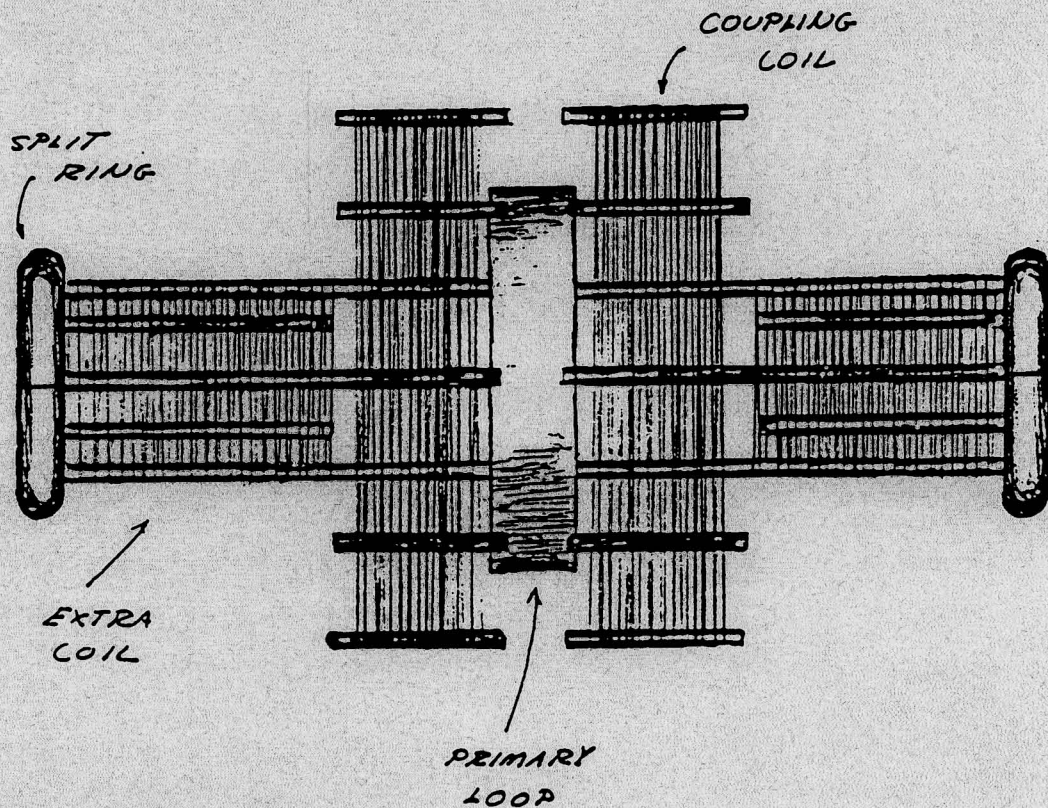


I) INTRODUCTION TO DIELECTRIC & MAGNETIC
DISCHARGES IN ELECTRICAL WINDINGS
by Eric Dollard, © 1982

II) ELECTRICAL OSCILLATIONS IN ANTENNAE
AND INDUCTION COILS
by John Miller, 1919



PART I

INTRODUCTION TO DIELECTRIC & MAGNETIC
DISCHARGES IN ELECTRICAL WINDINGS

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2. CAPACITANCE INADEQUATELY EXPLAINED
3. LINES OF FORCE AS REPRESENTATION OF DIELECTRICITY
4. THE LAWS OF LINES OF FORCE
5. FARADAY'S LINES OF FORCE THEORY
6. PHYSICAL CHARACTERISTICS OF LINES OF FORCE
7. MASS ASSOCIATED WITH LINES OF FORCE IN MOTION
8. INDUCTANCE AS AN ANALOGY TO CAPACITANCE
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10. THE LIMITS ZERO AND INFINITY
11. INSTANT ENERGY RELEASE AS INFINITY
12. ANOTHER FORM OF ENERGY APPEARS
13. ENERGY STORAGE SPATIALLY DIFFERENT THAN MAGNETIC ENERGY STORAGE
14. VOLTAGE IS TO DIELECTRICITY AS CURRENT IS TO MAGNETISM
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PART II

ELECTRICAL OSCILLATIONS IN ANTENNAE & INDUCTION COILS

J.M. Miller

Proceedings, Institute of Radio Engineers, 1919



P.O. BOX 429 ★ GARBERVILLE, CA 95440-0429 ★ U.S.A.

1. CAPACITANCE

The phenomena of capacitance is a type of electrical energy storage in the form of a field in an enclosed space. This space is typically bounded by two parallel metallic plates or two metallic foils on an intervening insulator or dielectric. A nearly infinite variety of more complex structures can exhibit capacity, as long as a difference in electric potential exists between various areas of the structure. The oscillating coil represents one possibility as to a capacitor of more complex form, and will be presented here.

2. CAPACITANCE INADEQUATELY EXPLAINED

The perception of capacitance as used today is wholly inadequate for the proper understanding of this effect. Steinmetz mentions this in his introductory book "Electric Discharges, Waves and Impulses". To quote, "Unfortunately, to a large extent in dealing with dielectric fields the prehistoric conception of the electrostatic charge (electron) on the conductor still exists, and by its use destroys the analogy between the two components of the electric field, the magnetic and the dielectric, and makes the consideration of dielectric fields unnecessarily complicated."

3. LINES OF FORCE AS REPRESENTATION OF DIELECTRICITY

Steinmetz continues, "There is obviously no more sense in thinking of the capacity current as current which charges the conductor with a quantity of electricity, than there is of speaking of the inductance voltage as charging the conductor with a quantity

of magnetism. But the latter conception, together with the notion of a quantity of magnetism, etc., has vanished since Faraday's representation of the magnetic field by lines of force."

4. THE LAWS OF LINES OF FORCE

All the lines of magnetic force are closed upon themselves, all dielectric lines of force terminate on conductors, but may form closed loops in electromagnetic radiation.

These represent the basic laws of lines of force. It can be seen from these laws that any line of force cannot just end in space.

5. FARADAY AND LINES OF FORCE THEORY

Faraday felt strongly that action at a distance is not possible thru empty space, or in other words, "matter cannot act where it is not." He considered space pervaded with lines of force. Almost everyone is familiar with the patterns formed by iron filings around a magnet. These filings act as numerous tiny compasses and orientate themselves along the lines of force existing around the poles of the magnet. Experiment has indicated that a magnetic field does possess a fibrous construct. By passing a coil of wire thru a strong magnetic field and listening to the coil output in headphones, the experimenter will notice a scraping noise. J. J. Thompson performed further experiments involving the ionization of gases that indicate the field is not continuous but fibrous (electricity and matter, 1906).

6. PHYSICAL CHARACTERISTICS OF LINES OF FORCE

Consider the space between poles of a magnet or capacitor as full of lines of electric force. See Fig. 1. These lines of force act as a quantity of stretched and mutually repellent springs. Anyone who has pushed together the like poles of two magnets has felt this springy mass. Observe Fig. 2. Notice the lines of force are more dense along $\overline{A B}$ in between poles, and that more lines on \overline{A} are facing B than are projecting outwards to infinity. Consider the effect of the lines of force on A. These lines are in a state of tension and pull on A. Because more are pulling on A towards B than those pulling on A away from B, we have the phenomena of physical attraction. Now observe Fig. 3. Notice now that the poles are like rather than unlike, more or all lines pull A away from B; the phenomena of physical repulsion.

7. MASS ASSOCIATED WITH LINES OF FORCE IN MOTION

The line of force can be more clearly understood by representing it as a tube of force or a long thin cylinder. Maxwell presented the idea that the tension of a tube of force is representative of electric force (volts/inch), and in addition to this tension, there is a medium through which these tubes pass. There exists a hydrostatic pressure against this media or ether. The value of this pressure is one half the product of dielectric and magnetic density. Then there is a pressure at right angles to an electric tube of force. If through the growth of a field the tubes of force spread sideways or in width, the broadside drag through

the medium represents the magnetic reaction to growth in intensity of an electric current. However, if a tube of force is caused to move endwise, it will glide through the medium with little or no drag as little surface is offered. This possibly explains why no magnetic field is associated with certain experiments performed by Tesla involving the movement of energy with no accompanying magnetic field.

8. INDUCTANCE AS AN ANALOGY TO CAPACITY

Much of the mystery surrounding the workings of capacity can be cleared by close examination of inductance and how it can give rise to dielectric phenomena. Inductance represents energy storage in space as a magnetic field. The lines of force orientate themselves in closed loops surrounding the axis of current flow that has given rise to them. The larger the space between this current and its images or reflections, the more energy that can be stored in the resulting field.

9. MECHANISM OF STORING ENERGY MAGNETICALLY

The process of pushing these lines or loops outward, causing them to stretch, represents storing energy as in a rubber band. A given current strength will hold a loop of force at a given distance from conductor passing current hence no energy movement. If the flow of current increases, energy is absorbed by the field as the loops are then pushed outward at a corresponding velocity. Because energy is in motion an E.M.F. must accompany the current flow in order for it to represent power. The magnitude of this EMF exactly corresponds to the velocity of the field. Then if the current

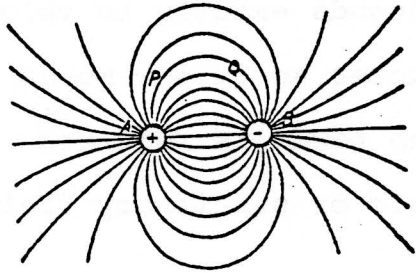


FIG. 2

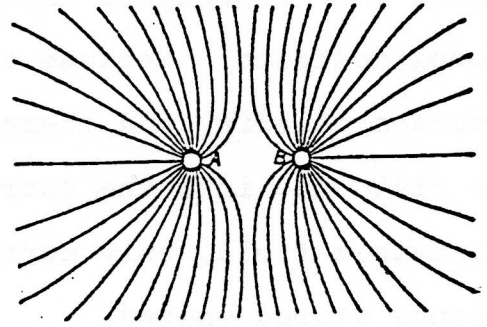


FIG. 3

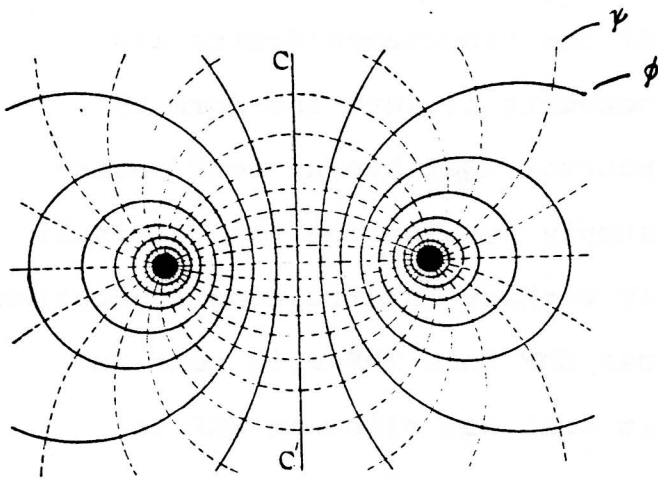


Fig. 1a — Electric Field of Circuit.

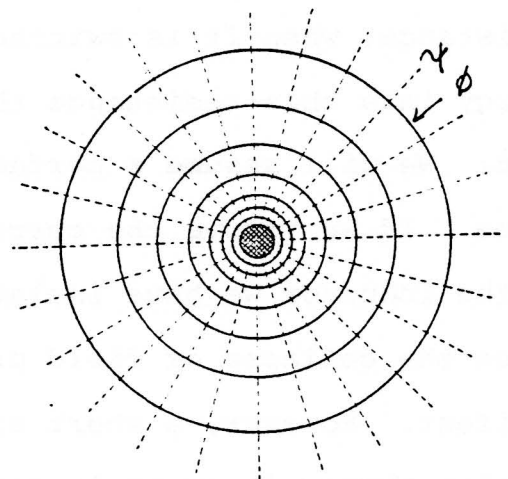


Fig. 1b — Electric Field of Conductor.

ceases changing in magnitude thereby becoming constant, no EMF accompanies it, as no power is being absorbed. However, if the current decreases and represents then a negative velocity of field as the loops contract. Because the EMF corresponds exactly to velocity it reverses polarity and thereby reverses power so it now moves out of the field and into the current. Since no power is required to maintain a field, only current, the static or stationary field, represents stored energy.

10. THE LIMITS OF ZERO AND INFINITY

Many interesting features of inductance manifest themselves in the two limiting cases of trapping the energy or releasing it instantly. Since the power supply driving the current has resistance, when it is switched off the inductance drains its energy into this resistance that converts it into the form of heat. We will assume a perfect inductor that has no self resistance. If we remove the current supply by shorting the terminals of the inductor we have isolated it without interrupting any current. Since the collapse of field produces EMF this EMF will tend to manifest. However, a short circuit will not allow an EMF to develop across it as it is zero resistance by definition. No EMF can combine with current to form power, therefore, the energy will remain in the field. Any attempt to collapse forces increased current which pushes it right back out. This is one form of storage of energy.

11. INSTANT ENERGY RELEASE AS INFINITY

Very interesting (and dangerous) phenomena manifest themselves when the current path is interrupted, thereby causing infinite resistance to appear. In this case resistance is best represented by its inverse, conductance. The conductance is then zero. Because the current vanished instantly the field collapses at a velocity approaching that of light. As EMF is directly related to velocity of flux, it tends towards infinity. Very powerful effects are produced because the field is attempting to maintain current by producing whatever EMF required. If a considerable amount of energy exists, say several kilowatt hours* (250 KWH for lightning stroke), the ensuing discharge can produce most profound effects and can completely destroy inadequately protected apparatus.

12. ANOTHER FORM OF ENERGY APPEARS

Through the rapid discharge of inductance a new force field appears that reduces the rate of inductive EMF formation. This field is also represented by lines of force but these are of a different nature than those of magnetism. These lines of force are not a manifestation of current flow but of an electric compression or tension. This tension is termed voltage or potential difference.

* The energy utilized by an average household in the course of one day.

13. DIELECTRIC ENERGY STORAGE SPATIALLY DIFFERENT THAN MAGNETIC ENERGY STORAGE

Unlike magnetism the energy is forced or compressed inwards rather than outwards. Dielectric lines of force push inward into internal space and along axis, rather than pushed outward broadside to axis as in the magnetic field. Because the lines are mutually repellent certain amounts of broadside or transverse motion can be expected but the phenomena is basically longitudinal. This gives rise to an interesting paradox that will be noticed with capacity. This is that the smaller the space bounded by the conducting structure the more energy that can be stored. This is the exact opposite of magnetism. With magnetism, the unit volumes of energy can be thought of as working in parallel but the unit volumes of energy in association with dielectricity can be thought of as working in series.

14. VOLTAGE IS TO DIELECTRICITY AS CURRENT IS TO MAGNETISM.

With inductance the reaction to change of field is the production of voltage. The current is proportionate to the field strength only and not velocity of field. With capacity the field is produced not by current but voltage. This voltage must be accompanied by current in order for power to exist. The reaction of capacitance to change of applied force is the production of current. The current is directly proportional to the velocity of field strength. When voltage increases a reaction current flows into capacitance and thereby energy accumulates. If voltage does not change no current flows and the capacitance stores the energy which produced the field. If the voltage decreases then the reaction current reverses and energy

flows out of the dielectric field.

As the voltage is withdrawn the compression within the bounded space is relieved. When the energy is fully dissipated the lines of force vanish.

15. AGAIN THE LIMITS ZERO AND INFINITY

Because the power supply which provides charging voltage has internal conductance, after it is switched off the current leaking through conductance drains the dielectric energy and converts it to heat. We will assume a perfect capacitance having no leak conductance. If we completely disconnect the voltage supply by open circuiting the terminals of the capacitor, no path for current flow exists by definition of an open circuit. If the field tends to expand it will tend towards the production of current. However, an open circuit will not allow the flow of current as it has zero conductance. Then any attempt towards field expansion raises the voltage which pushes the field back inwards. Therefore, energy will remain stored in the field. This energy can be drawn for use at any time. This is another form of energy storage.

16. INSTANT ENERGY RELEASE AS INFINITY

Phenomena of enormous magnitude manifest themselves when the criteria for voltage or potential difference is instantly disrupted, as with a short circuit. The effect is analogous with the open circuit of inductive current. Because the forcing voltage is instantly withdrawn the field explodes against the bounding conductors with a velocity that may exceed light. Because the current is directly related to the velocity of field it jumps to infinity in its attempt to produce

finite voltage across zero resistance. If considerable energy had resided in the dielectric force field, again let us say several K.W.H. the resulting explosion has almost inconceivable violence and can vaporize a conductor of substantial thickness instantly. Dielectric discharges of great speed and energy represent one of the most unpleasant experiences the electrical engineer encounters in practice.

17. ENERGY RETURNS TO MAGNETIC FORM

The powerful currents produced by the sudden expansion of a dielectric field naturally give rise to magnetic energy. The inertia of the magnetic field limits the rise of current to a realistic value. The capacitance dumps all its energy back into the magnetic field and the whole process starts over again. The inverse of the product of magnetic storage capacity and dielectric storage capacity represents the frequency or pitch at which this energy interchange occurs. This pitch may or may not contain overtones depending on the extent of conductors bounding the energies.

18. CHARACTERISTIC IMPEDANCE AS REPRESENTATION OF PULSATION OF ENERGY FIELD

The ratio of magnetic storage ability to that of the dielectric is called the characteristic impedance. This gives the ratio of maximum voltage to maximum current in the oscillatory structure. However, as the magnetic energy storage is outward and the dielectric storage is inward the total or double energy field pulsates in shape or size. The axis of this pulsation of force is the impedance of the system displaying oscillations and pulsation occurs at the frequency of oscillation.

19. ENERGY INTO MATTER

As the voltage or impedance is increased the emphasis is on the inward flux. If the impedance is high and rate of change is fast enough (perfect overtone series), it would seem possible the compression of the energy would transform it into matter and the reversion of this matter into energy may or may not synchronize with the cycle of oscillation. This is what may be considered supercapacitance, that is, stable longterm conversion into matter.

20. MISCONCEPTIONS OF PRESENT THEORY OF CAPACITANCE

The misconception that capacitance is the result of accumulating electrons has seriously distorted our view of dielectric phenomena. Also the theory of the velocity of light as a limit of energy flow, while adequate for magnetic force and material velocity, limits our ability to visualize or understand certain possibilities in electric phenomena. The true workings of free space capacitance can be best illustrated by the following example. It has been previously stated that dielectric lines of force must terminate on conductors. No line of force can end in space. If we take any conductor and remove it to the most remote portion of the universe, no lines of force can extend from this electrode to other conductors. It can have no free space capacity, regardless of the size of the electrode, therefore it can store no energy. This indicates that the free space capacitance of an object is the sum mutual capacity of it to all the conducting objects of the universe.

21. FREE SPACE INDUCTANCE IS INFINITE

Steinmetz in his book on the general or unified behavior of electricity "The Theory and Calculation of Transient Electric Phenomena and Oscillation," points out that the inductance of any unit length of an isolated filamentary conductor must be infinite. Because no image currents exist to contain the magnetic field it can grow to infinite size. This large quantity of energy cannot be quickly retrieved due to the finite velocity of propagation of the magnetic field. This gives a non reactive or energy component to the inductance which is called electromagnetic radiation.

22. WORK OF TESLA, STEINMETZ AND FARADAY

In the aforementioned books of Steinmetz he develops some rather unique equations for capacity. Tesla devoted an enormous portion of his efforts to dielectric phenomena and made numerous remarkable discoveries in this area. Much of this work is yet to be fully uncovered. It is my contention that the phenomena of dielectricity is wide open for profound discovery. It is ironic that we have abandoned the lines of force concept associated with a phenomena measured in the units called farads after Farady, whose insight into forces and fields has led to the possibility of visualization of the electrical phenomena.

IMPORTANT REFERENCE MATERIAL

1. "Electricity and Matter," J. J. Thompson
New York, 1906, Scribner's Sons, and 1904, Yale University
2. "Elementary Lectures on Electric Discharges, Waves, and
Impulses and other Transients." C. P. Steinmetz, second
edition, 1914, McGraw-Hill
3. "Theory and Calculation of Transient Electric Phenomena
and Oscillations," C. P. Steinmetz, third edition, 1920,
McGraw-Hill. Section III Transients in Space, Chapter VIII,
Velocity of Propagation of Electric Field.

23. QUESTION AS TO THE VELOCITY OF DIELECTRIC FLUX

It has been stated that all magnetic lines of force must be closed upon themselves, and that all dielectric lines of force must terminate upon a conducting surface. It can be inferred from these two basic laws that no line of force can terminate in free space. This creates an interesting question as to the state of dielectric flux lines before the field has had time to propagate to the neutral conductor. During this time it would seem that the lines of force, not having reached the distant neutral conductor would end in space at their advancing wave front. It could be concluded that either the lines of force propagate instantly or always exist and are modified by the electric force, or voltage. It is possible that additional or conjugate space exists within the same boundaries as ordinary space. The properties of lines of force within this conjugate space may not obey the laws of normally conceived space.

TABLE I.

Magnetic Field.	Dielectric Field.
Magnetic flux: $\Phi = Li$ 10^8 lines of magnetic force.	Dielectric flux: $\Psi = Ce$ lines of dielectric force, or coulombs.
Inductance voltage: $e' = n \frac{d\Phi}{dt} 10^{-8} = L \frac{di}{dt}$ volts.	Capacity current: $i' = \frac{d\Psi}{dt} = C \frac{de}{dt}$ amperes.
Magnetic energy: $w = \frac{Li^2}{2}$ joules.	Dielectric energy: $w = \frac{Ce^2}{2}$ joules.
Magnetomotive force: $F = ni$ ampere turns.	Electromotive force: $e =$ volts.
Magnetizing force: $f = \frac{F}{l}$ ampere turns per cm.	Electrifying force or voltage gradient: $G = \frac{e}{l}$ volts per cm.
Magnetic-field intensity: $\mathcal{H} = 4\pi f 10^{-1}$ lines of magnetic force per cm^2 .	Dielectric-field intensity: $K = \frac{G}{4\pi e^2} 10^9$ lines of dielectric force per cm^2 , or coulombs per cm^2 .
Magnetic density: $\mathcal{B} = \mu\mathcal{H}$ lines of magnetic force per cm^2 .	Dielectric density: $D = \kappa K$ lines of dielectric force per cm^2 , or coulombs per cm^2 .
Permeability: μ	Permittivity or specific capacity: κ
Magnetic flux: $\Phi = A\mathcal{B}$ lines of magnetic force.	Dielectric flux: $\Psi = AD$ lines of dielectric force, or coulombs.

$v = 3 \times 10^{10} =$ velocity of light.

TABLE II.

Magnetic Circuit.	Dielectric Circuit.	Electric Circuit.
Magnetic flux (magnetic current): Φ = lines of magnetic force.	Dielectric flux (dielectric current): Ψ = lines of dielectric force.	Electric current: i = electric current.
Magnetomotive force: F = ni ampere turns.	Electromotive force: e = volts.	Voltage: e = volts.
Permeance: $M = \frac{\Phi}{.4\pi F}$.	Permittance or capacity: $C = \frac{\Psi}{e}$ farads.	Conductance: $g = \frac{i}{e}$ mhos.
Inductance: $L = \frac{n^2\Phi}{F} 10^{-9} = \frac{n\Phi}{i} 10^{-9}$ henry.	(Elastance): $\frac{1}{C} = \frac{e}{\Psi}$.	Resistance: $r = \frac{e}{i}$ ohms.
Reluctance: $R = \frac{F}{\Phi}$.	Dielectric energy: $w = \frac{Ce^2}{2} = \frac{e\Psi}{2}$ joules.	Electric power: $p = ri^2 = ge^2 = ei$ watts.
Magnetic energy: $w = \frac{Li^2}{2} = \frac{F\Phi}{2} 10^{-9}$ joules.	Dielectric density: $D = \frac{\Psi}{A} = \kappa K$ lines per cm ² .	Electric-current density: $I = \frac{i}{A} = \gamma G$ amperes per cm ² .
Magnetic density: $\mathcal{B} = \frac{\Phi}{A} = \mu \mathcal{K}$ lines per cm ² .	Dielectric gradient: $G = \frac{e}{l}$ volts per cm.	Electric gradient: $G = \frac{e}{l}$ volts per cm.
Magnetizing force: $f = \frac{F}{l}$ ampere turns per cm.	Dielectric-field intensity: $K = \frac{G}{4\pi v^2} 10^9$.	Conductivity: $\gamma = \frac{I}{G}$ mho-cm.
Magnetic-field intensity: $\mathcal{H} = .4\pi f$.	Permittivity or specific capacity: $\kappa = \frac{D}{K}$.	Resistivity: $\rho = \frac{1}{\gamma} = \frac{G}{I}$ ohm-cm.
Permeability: $\mu = \frac{\mathcal{B}}{\mathcal{H}}$.	(Elastivity ?): $\frac{1}{\kappa} = \frac{K}{D}$.	Specific power: $p_0 = \rho I^2 = G^2 = GI$ watts per cm ² .
Reluctivity: $\rho = \frac{f}{\mathcal{B}}$.	Specific dielectric energy: $w_0 = \frac{\kappa G^2}{4\pi v^2} 10^9 = \frac{GD}{2} 10^9 = \frac{2\pi v^2 KD}{2\pi v^2} 10^9$ joules per cm ² .	
Specific magnetic energy: $w_0 = \frac{.4\pi\mu f^2}{2} = \frac{f\mathcal{B}}{2} 10^{-3} = \frac{\mathcal{H}\mathcal{B}}{8\pi} 10^{-7}$ joules per cm ² .		

APPENDIX I

TABLE OF UNITS, SYMBOLS, AND DIMENSIONS

Quantity	Symbol	mks Unit Rationalized	Defining Equation	Dimensional Formula Exponents of				cgs emu	No. of emu No. of mks	cgs esu	No. of esu No. of mks	No. of esu No. of emu
				L	M	T	Q					
1 Length	L	m		1	0	0	0	cm	10 ²	cm	10 ²	1
2 Area	A	m ²	A = L ²	2	0	0	0	cm ²	10 ⁴	cm ²	10 ⁴	1
3 Volume	V	m ³	V = L ³	3	0	0	0	cm ³	10 ⁶	cm ³	10 ⁶	1
4 Mass	M, m	kilogram		0	1	0	0	gram	10 ³	gram	10 ³	1
5 Time	T, t	second		0	0	1	0	second	1	second	1	1
6 Velocity	v	m/sec	v = L/T	1	0	-1	0	cm/sec	10 ²	cm/sec	10 ²	1
7 Acceleration	a	m/sec ²	a = L/T ²	1	0	-2	0	cm/sec ²	10 ⁴	cm/sec ²	10 ⁴	1
8 Force	F	newton	F = Ma	1	1	-2	0	dyne	10 ⁵	dyne	10 ⁵	1
9 Energy	W	joule	W = FL	2	1	-2	0	erg/sec	10 ⁷	erg/sec	10 ⁷	1
10 Power	P	watt	P = W/T	2	1	-3	0	erg/sec	10 ⁷	erg/sec	10 ⁷	1
11 Charge	Q, q	coulomb	P = Q ² /(4πε ₀ L ²)	0	0	0	1	abercoulomb	10 ⁻¹	statcoulomb	10 ⁹	100c
12 Dielectric constant of free space	ε ₀	farad/m	ε ₀ = 1/(μ ₀ c ²)	-3	-1	2	2			1	4πc ² /10 ⁹	
13 Dielectric constant relative	ε _r	farad/m		-3	-1	2	2					
14 Charge density	σ	numeric	ε _r = ε/ε ₀	0	0	0	0				1	
15 volume	ρ	coulomb/m ³	ρ = Q/V	-3	0	0	1	abercoulomb/cm ³	10 ⁻⁷	statcoulomb/cm ³	c/10 ⁹	100c
16 surface	ρ _s	coulomb/m ²	ρ _s = Q/A	-2	0	0	1	abercoulomb/cm ²	10 ⁻⁵	statcoulomb/cm ²	c/10 ⁷	100c
17 line	ρ _l	coulomb/m	ρ _l = Q/L	-1	0	0	1	abercoulomb/cm	10 ⁻³	statcoulomb/cm	c/10 ⁵	100c
18 Electric intensity	E	volt/m	E = F/Q = -V/L	1	1	-2	-1	abvolt/cm	10 ⁸	statvolt/cm	10 ⁸ /c	1/(100c)
19 Electric flux density	D	coulomb/m ²	D = εE = ψ/A	-2	0	0	1		4π × 10 ⁹		4πc/10 ⁹	100c
20 Electric flux	ψ	coulomb	ψ = DA	0	0	0	1		4π × 10 ⁹		4π10c	100c
21 Electric potential	V	volt	V = -EL	2	1	-2	-1	abvolt	10 ⁸	statvolt	10 ⁸ /c	1/(100c)
22 EMF	V _e	volt	V _e = -∫db/dt	2	1	-2	-1	abvolt	10 ⁸	statvolt	10 ⁸ /c	1/(100c)
23 Capacitance	C	farad	C = Q/V	-2	-1	2	2	abfarad	10 ⁻⁹	statfarad	c ² /10 ⁹	(100c) ²
24 Current	I, i	ampere	I = Q/T	0	0	-1	1	abampere	10 ⁻¹	statampere	10c	100c
25 Current density	J	ampere/m ²	J = I/A	-2	0	-1	1	abampere/cm ²	10 ⁻³	statampere/cm ²	c/10 ⁷	100c
26 Resistance	R	ohm	R = V/I	2	1	-1	-2	abohm	10 ¹¹	statohm	10 ¹¹ /c	1/(100c) ²
27 Resistivity	ρ	ohm-m	ρ = RA/L	3	1	-1	-2	abohm-cm	10 ¹³	statohm-cm	10 ¹³ /c	1/(100c) ²
28 Conductance	G	mho	G = 1/R	-2	-1	1	2	abmho	10 ⁻⁹	statmho	c ² /10 ⁹	(100c) ²
29 Conductivity	σ	mho/m	σ = 1/ρ = J/E	-2	-1	1	2	abmho/cm	10 ⁻¹¹	statmho/cm	c ² /10 ⁹	(100c) ²
30 Electric polarization	P	coulomb/m ²	P = D - ε ₀ E = ρL	-2	0	0	1	abercoulomb/cm ²	10 ⁻⁵	statcoulomb/cm ²	c/10 ⁷	100c
31 Electric susceptibility	χ _e	farad/m	χ _e = P/E = ε ₀ (ε _r - 1)	-3	-1	2	2			1	4πc ² /10 ⁹	
32 Electric dipole moment	m _e	coulomb-m	m _e = QL	1	0	0	1				10 ⁹ c	
33 Electric energy density	w _e	joule/cm ³	w _e = DE/2	-1	1	-2	0	erg/cm ³	1	statcoulomb-cm erg/cm ³	10 ⁹ c	1

TABLE OF UNITS, SYMBOLS, AND DIMENSIONS

Quantity	Symbol	mks Unit Rationalized	Defining Equation	Dimensional Formula Exponents of				cgs emu	No. of emu No. of mks	cgs esu	No. of esu No. of mks	No. of esu No. of emu
				L	M	T	Q					
34 Permeability of free space	μ ₀	henry/m	μ ₀ = 4π/10 ⁷	1	1	0	-2		10 ⁷ /4π			
35 Permeability relative	μ _r	numeric	μ _r = B/H	1	1	0	-2			1		
36 Magnetic pole	ρ	weber	ρ = μ/μ ₀	0	0	0	0					
37 Magnetic pole	p	weber	p = A(B - B ₀)	2	1	-1	-1					
38 Magnetic moment	m	weber-m	m = ρL	3	1	-1	-1	pole	10 ⁸ /4π			
39 Magnetic intensity	H	ampere/m or newton/weber	H = U/L or F/ρ	-1	0	-1	1	maxwell/4π pole-cm oersted or gilbert/cm	10 ⁹ /4π			
40 Magnetic flux density	B	weber/m ²	B = μH = φ/A	0	1	-1	-1	gauss or maxwell/cm ²	10 ⁸			
41 Magnetic flux	φ	weber	φ = BA = ∫ _S B · dA	2	1	-1	-1	maxwell	10 ⁸			
42 Magnetic potential	U	ampere	U = ∫ H · dl	0	0	-1	1	gilbert	4π/10			
43 MMF	F	ampere	F = I	0	0	-1	1	gilbert	4π/10			
44 Intensity of magnetization	M	weber/m ²	M = B - B ₀ = m/L ³	0	1	-1	-1	pole/cm ² or gauss/4π	10 ⁸ /4π			
45 Inductance self	L	henry	L = φ/I	2	1	0	-2	abhenry	10 ⁹			
46 mutual	M	henry	M = φ ₂ /I ₁ = W/I ²	2	1	0	-2	abhenry	10 ⁹			
47 Reluctance	R	ampere/weber	R = F/φ	-2	-1	0	2				10 ⁹ /c ²	1/(100c) ²
48 Reluctivity	ρ	meter/henry	ρ = 1/μ	-1	-1	0	2					
49 Permeance	P	weber/amp	P = 1/ρ	2	1	0	-2					
50 Permittivity	ε	henry/meter	ε = 1/ρ	2	1	0	-2					
51 EMF	V _e	volt	V _e = -∫db/dt	2	1	-2	-1	abvolt	10 ⁸	statvolt	10 ⁸ /c	1/(100c)
52 Poynting's vector	S	watts/m ²	S = EH	0	1	-3	0	abwatt/cm ²	10 ³	statwatt/cm ²	10 ³	1
53 Magnetic energy density	w _m	joule/m ³	w _m = HB/2	-1	1	-2	0	erg/cm ³	10	erg/cm ³	10	1
54 Magnetic susceptibility	χ _m	henry/m	χ _m = M/H = μ _r (μ _r - 1)	1	1	0	-2	henry/m	10 ⁷ /4π			

μ₀ = 4π/10⁷ henrys/meter. For c = 2.998 × 10⁸ meters/sec, ε₀ = 1/μ₀c² = 10⁷/(4πc²) = 8.854 × 10⁻¹² farad/meter
 For c ≈ 3 × 10⁸ meters/sec, ε₀ ≈ 1/(36π10⁹) farad/meter
 c² = 8.988 × 10¹⁶ ≈ 9 × 10¹⁶

I. INTRODUCTION

In the following paper are outlined some results of the application of the theory of circuits having uniformly distributed electrical characteristics to the electrical oscillations in antennas and inductance coils. Experimental methods are also given for determining the constants of antennas and experimental results showing the effect of imperfect dielectrics upon antenna resistance.

The theory of circuits having uniformly distributed characteristics such as cables, telephone lines, and transmission lines has been applied to antennas by a number of authors. The results of the theory do not seem to have been clearly brought out, and in fact erroneous results have at times been derived and given prominence in the literature. As an illustration, in one article the conclusion has been drawn that the familiar method of determining the capacity and inductance of antennas by the insertion of two known loading coils leads to results which are in very great error. In the following treatment it is shown that this is not true and that the method is very valuable.

Another point concerning which there seems to be considerable uncertainty is that of the effective values of the capacity, inductance and resistance of antennas. In this paper expressions are obtained for these quantities giving the values which would be suitable for an artificial antenna to represent the actual antenna at a given frequency.

The theory is applied also to the case of inductance coils with distributed capacity in which case an explanation of a well-known experimental result is obtained.

Experimental methods are given for determining the constants of antennas, the first of which is the familiar method previously mentioned. It is shown that this method in reality gives values of capacity and inductance of the antenna close to the low frequency or static values and may be corrected so as to give these values very accurately. The second method concerns the determination of the effective values of the capacity, inductance, and resistance of the antenna.

In the portion which deals with the resistance of antennas, a series of experimental results are given which explain the linear rise in resistance of antennas as the wave length is increased. It is shown that this characteristic feature of antenna resistance curves is caused by the presence of imperfect dielectric such as trees, buildings, and so on, in the field of the antenna, which causes it to behave as an absorbing condenser.

II. CIRCUIT WITH UNIFORMLY DISTRIBUTED INDUCTANCE AND CAPACITY

The theory, generally applicable to all circuits with uniformly distributed inductance and capacity, will be developed for the case of two parallel wires. The wires (Figure 1) are of length l and of low resistance. The inductance per unit length

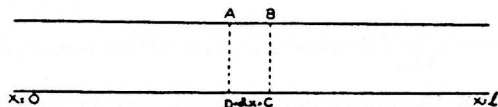


FIGURE 1

L_1 is defined by the flux of magnetic force between the wires per unit of length that there would be if a steady current of one ampere were flowing in opposite directions in the two wires. The capacity per unit length C_1 is defined by the charge that there would be on a unit length of one of the wires if a constant emf. of one volt were impressed between the wires. Further the quantity $L_0 = l L_1$ would be the total inductance of the circuit if the current flow were the same at all parts. This would be the case if a constant or slowly alternating voltage were applied at $x=0$ and the far end ($x=l$) short-circuited. The quantity $C_0 = l C_1$ would represent the total capacity between the wires if a constant or slowly alternating voltage were applied at $x=0$ and the far end were open.

Let us assume, without defining the condition of the circuit at $x=l$, that a sinusoidal emf. of periodicity $\omega = 2\pi f$ is impressed at $x=0$ giving rise to a current of instantaneous value i at A and a voltage between A and D equal to v . At B the current will be $i + \frac{\partial i}{\partial x} dx$ and the voltage from B to C will be $v + \frac{\partial v}{\partial x} dx$.

The voltage around the rectangle $ABCD$ will be equal to the rate of decrease of the induction thru the rectangle; hence

$$\begin{aligned} \left(v + \frac{\partial v}{\partial x}\right) dx - v &= -\frac{\partial}{\partial t} (L_1 i dx) \\ \frac{\partial v}{\partial x} &= -L_1 \frac{\partial i}{\partial t} \end{aligned} \quad (1)$$

Further the rate of increase of the charge q on the elementary length of wire AB will be equal to the excess in the current flowing in at A over that flowing out at B .

Hence

$$\frac{\partial q}{\partial t} = \frac{\partial}{\partial t} (C_1 v dx) = i - \left(i + \frac{\partial i}{\partial x} dx \right) - \frac{\partial i}{\partial x} = C_1 \frac{\partial v}{\partial t} \quad (2)$$

These equations (1) and (2), determine the propagation of the current and voltage waves along the wires. In the case of sinusoidal waves, the expressions

$$v = \cos \omega t (A \cos \omega \sqrt{C_1 L_1} x + B \sin \omega \sqrt{C_1 L_1} x) \quad (3)$$

$$i = \sin \omega t \sqrt{\frac{C_1}{L_1}} (A \sin \omega \sqrt{C_1 L_1} x - B \cos \omega \sqrt{C_1 L_1} x) \quad (4)$$

are solutions of the above equations as may be verified by substitution. The quantities A and B are constants depending upon the terminal conditions. The velocity of propagation of the waves at high frequencies, is

$$V = \frac{1}{\sqrt{L_1 C_1}}$$

III. THE ANTENNA

1. REACTANCE OF THE AERIAL-GROUND PORTION

The aerial-ground portion of the antenna (CD in Figure 2) will be treated as a line with uniformly distributed inductance, capacity and resistance. As is common in the treatment of

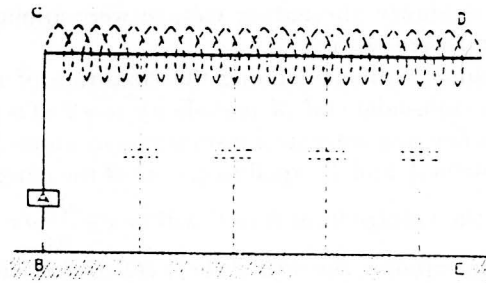


FIGURE 2—Antenna Represented as a Line with Uniform Distribution of Inductance and Capacity

radio circuits, the resistance will be considered to be so low as not to affect the frequency of the oscillations or the distribution of current and voltage. The lead-in BC (Figure 2) will be

considered to be free from inductance or capacity excepting as inductance coils or condensers are inserted (at A) to modify the oscillations.

Applying equations (3) and (4) to the aerial of the antenna and assuming that $x=0$ is the lead-in end while $x=l$ is the far end which is open, we may introduce the condition that the current is zero for $x=l$. From (4)

$$\frac{A}{B} = \cot \omega \sqrt{C_1 L_1} l \quad (5)$$

Now the reactance of the aerial, which includes all of the antenna but the lead-in, is given by the current and voltage at $x=0$. These are, from (3), (4), and (5),

$$v_a = A \cos \omega t = B \cot \omega \sqrt{C_1 L_1} l \cos \omega t$$

$$i_a = -\sqrt{\frac{C_1}{L_1}} B \sin \omega t$$

The current leads the voltage when the cotangent is positive, and lags when the cotangent is negative. The reactance of the aerial, given by the ratio of the maximum values of v_a to i_a is

$$X = -\sqrt{\frac{L_1}{C_1}} \cot \omega \sqrt{C_1 L_1} l$$

or in terms of $C_a = l C_1$ and $L_a = l L_1$

$$X = -\sqrt{\frac{L_a}{C_a}} \cot \omega \sqrt{C_a L_a} \quad (6)$$

or since $V = \frac{1}{\sqrt{L_1 C_1}}$

$$X = -L_1 V \cot \omega \sqrt{C_1 L_1} l$$

as given by J. S. Stone.¹

At low frequencies the reactance is negative and hence the aerial behaves as a capacity. At the frequency $f = \frac{1}{4\sqrt{C_a L_a}}$ the reactance becomes zero and beyond this frequency is positive or inductive up to the frequency $f = \frac{1}{2\sqrt{C_a L_a}}$, at which the reactance becomes infinite. This variation of the aerial reactance with the frequency is shown by the cotangent curves in Figure 3.

¹Stone, J. S.: "Trans. Int. Elec. Congress," St. Louis, 3, p. 555; 1904.

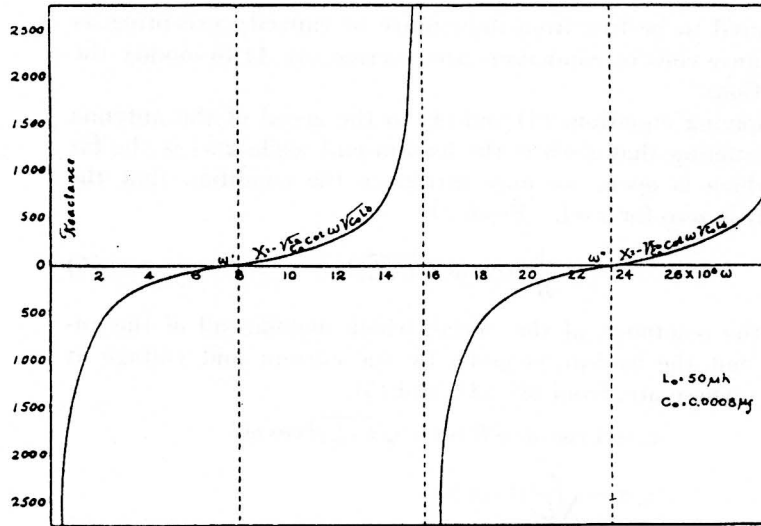


FIGURE 3—Variation of the Reactance of the Aerial of an Antenna with the Frequency

2. NATURAL FREQUENCIES OF OSCILLATION

Those frequencies at which the reactance of the aerial, as given by equation (6), becomes equal to zero are the natural frequencies of oscillation of the antenna (or frequencies of resonance) when the lead-in is of zero reactance. They are given in Figure 3 by the points of intersection of the cotangent curves with the axis of ordinates and by the equation

$$f = \frac{m}{4\sqrt{C_0 L_0}}; \quad m = 1, 3, 5, \text{ etc.}$$

The corresponding wave lengths are given by

$$\lambda = \frac{V}{f} = \frac{l}{f\sqrt{C_0 L_0}} = \frac{4l}{m}$$

i. e., $4/1, 4/3, 4/5, 4/7, \text{ etc.}$, times the length of the aerial. If, however, the lead-in has a reactance X_r , the natural frequencies of oscillation are determined by the condition that the total reactance of lead-in plus aerial shall be zero, that is:

$$X_r + X = 0$$

provided the reactances are in series with the driving emf.

(a) **LOADING COIL IN LEAD-IN.** The most important practical case is that in which an inductance coil is inserted in the

lead-in. If the coil has an inductance L its reactance $X_L = \omega L$. This is a positive reactance increasing linearly with the frequency and represented in Figure 4 by a solid line. Those frequencies at which the reactance of the coil is equal numerically but opposite in sign to the reactance of the aerial, are the natural frequencies of oscillation of the loaded antenna since the total reactance $X_L + X = 0$. Graphically these frequencies are deter-

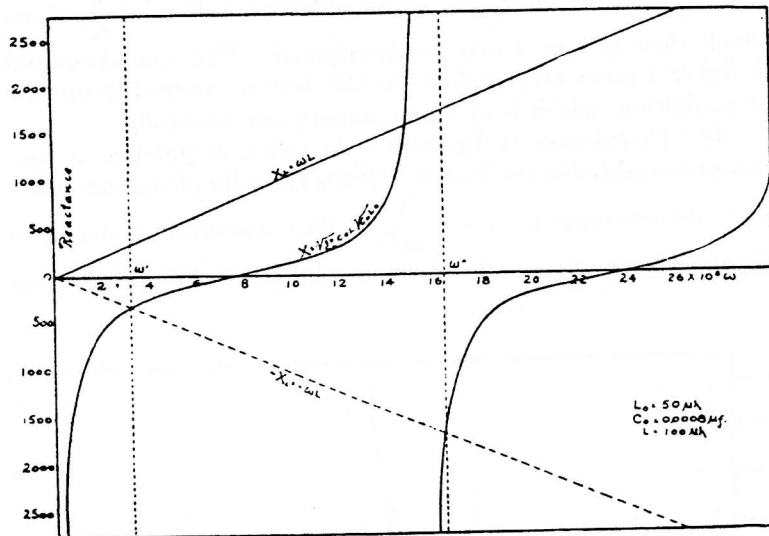


FIGURE 4—Curves of Aerial and Loading Coil Reactances

mined by the intersection of the straight line $-X_L = -\omega L$ (shown by a dashed line in Figure 4) with the cotangent curves representing X . It is evident that the frequency is lowered by the insertion of the loading coil and that the higher natural frequencies of oscillation are no longer integral multiples of the lowest frequency.

The condition $X_L + X = 0$ which determines the natural frequencies of oscillation leads to the equation

$$\omega L - \frac{L_0}{\sqrt{C_0}} \cot \omega \sqrt{C_0 L_0} = 0$$

OR

$$\cot \omega \sqrt{C_0 L_0} = \frac{L}{L_0} \quad (8)$$

This equation has been given by Guyau² and L. Cohen.³ It determines the periodicity ω and hence the frequency and wave length of the possible natural modes of oscillation when the distributed capacity and inductance of the aerial and the inductance of the loading coil are known. This equation cannot, however, be solved directly; it may be solved graphically as shown in Figure 4 or a table may be prepared indirectly which gives the values of $\omega \sqrt{C_o L_o}$ for different values of $\frac{L_c}{L_o}$, from which then ω , f or λ may be determined. The second column of Table I gives these values for the lowest natural frequency of oscillation, which is of major importance naturally.

(b) CONDENSER IN LEAD-IN. At times, in practice, a condenser is inserted in the lead-in. If the capacity of the condenser is C , its reactance is $X_c = -\frac{1}{\omega C}$. This reactance is shown in Figure 5 by the hyperbola drawn in solid line. The intersection

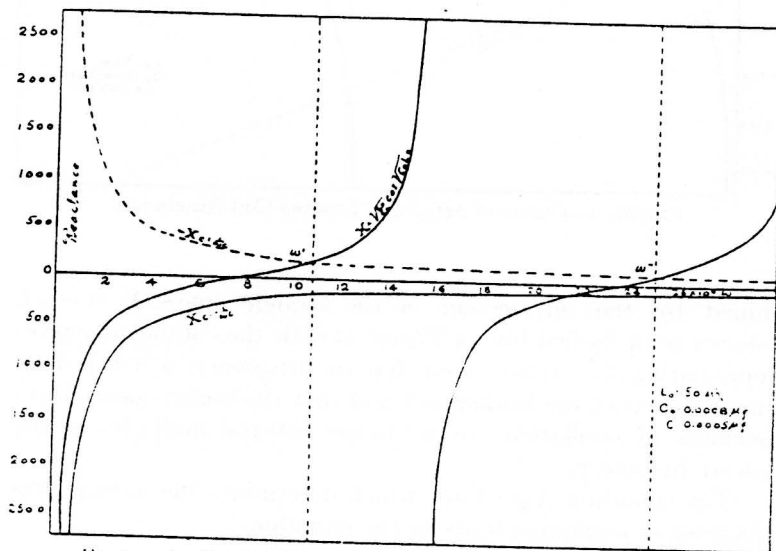


FIGURE 5—Curves of Aerial and Series Condenser Reactances

of the negative of this curve (drawn in dashed line) with the cotangent curves representing X gives the frequencies for which

²Guyau, A.; "Lumière Electrique," 15, p. 13; 1911.

³Cohen, L.; "Electrical World," 65, p. 286; 1915.

TABLE I

DATA FOR LOADED ANTENNA CALCULATIONS

$\frac{L}{L_0}$	$\omega \sqrt{C_0 L_0}$	$\frac{1}{\sqrt{\frac{L}{L_0} + 3}}$	Difference, per cent	$\frac{L}{L_0}$	$\omega \sqrt{C_0 L_0}$	$\frac{1}{\sqrt{\frac{L}{L_0} + 3}}$	Difference, per cent
0.0	1.571	1.732	10.3	3.1	0.539	0.540	0.1
.1	1.429	1.519	6.3	3.2	.532	.532	.1
.2	1.314	1.369	4.2	3.3	.524	.525	.1
.3	1.220	1.257	3.0	3.4	.517	.518	.1
.4	1.142	1.168	2.3	3.5	.510	.511	.1
.5	1.077	1.095	1.7	3.6	.504	.504	.0
.6	1.021	1.035	1.4	3.7	.4977	.4979	.0
.7	.973	.984	1.1	3.8	.4916	.4919	.0
.8	.931	.939	.9	3.9	.4859	.4860	.0
.9	.894	.900	.7	4.0	.4801	.4804	.0
1.0	.860	.866	.7	4.5	.4548	.4519	.0
1.1	.831	.835	.5	5.0	.4330	.4330	.0
1.2	.804	.808	.5	5.5	.4141
1.3	.779	.782	.4	6.0	.3974
1.4	.757	.760	.4	6.5	.3826
1.5	.736	.739	.4	7.0	.3693
1.6	.717	.719	.3	7.5	.3574
1.7	.699	.701	.3	8.0	.3465
1.8	.683	.685	.3	8.5	.3366
1.9	.668	.680	.3	9.0	.3275
2.0	.653	.655	.3	9.5	.3189
2.1	.640	.641	.2	10.0	.3111
2.2	.627	.628	.2	11.0	.2972
2.3	.615	.616	.2	12.0	.2850
2.4	.604	.605	.2	13.0	.2741
2.5	.593	.594	.2	14.0	.2644
2.6	.583	.584	.2	15.0	.2556
2.7	.574	.574	.2	16.0	.2476
2.8	.564	.565	.1	17.0	.2402
2.9	.556	.556	.1	18.0	.2338
3.0	.547	.548	.1	19.0	.2277
				20.0	.2219

$X_c + X = 0$, and hence the natural frequencies of oscillation of the antenna. The frequencies are increased (the wave length decreased) by the insertion of the condenser and the oscillations of higher frequencies are not integral multiples of the lowest.

The condition $X_c + X = 0$ is expressed by the equation

$$-\frac{\tan \omega \sqrt{C_o L_o}}{\omega \sqrt{C_o L_o}} = \frac{C}{C_o} \quad (9)$$

which has been given by Guyau. Equation (9) may be solved graphically as above or a table similar to Table I may be prepared giving $\omega \sqrt{C_o L_o}$ for different values of $\frac{C}{C_o}$. More complicated circuits may be solved in a similar manner.

3. EFFECTIVE RESISTANCE, INDUCTANCE, AND CAPACITY

In the following, the most important practical case of a loading coil in the lead-in and the natural oscillation of lowest frequency will alone be considered. The problem is to replace the antenna of Figure 6 (a) which has a loading coil L in the lead-in and an aerial with distributed characteristics by a circuit Figure 6 (b) consisting of the inductance L in series with lumped resistance R_e , inductance L_e , capacity C_e , which are equivalent to the aerial. It is necessary, however, to state how these effective values are to be defined.

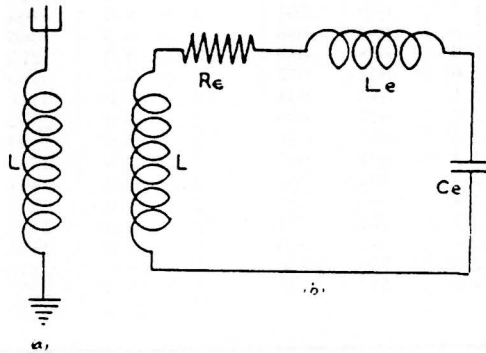


FIGURE 6

In practice the quantities which are of importance in an antenna are the resonant wave length or frequency and the current at the current maximum. The quantities L_e and C_e are, therefore, defined as those which will give the circuit (b) the

same resonant frequency as the antenna in (a). Further the three quantities L_e , C_e , and R_e must be such that the current in (b) will be the same as the maximum in the antenna for the same applied emf. whether undamped or damped with any decrement. These conditions determine L_e , C_e , and R_e uniquely at any given frequency, and are the proper values for an artificial antenna which is to represent an actual antenna at a particular frequency. In the two circuits the corresponding maxima of magnetic energies and electrostatic energies and the dissipation of energy will be the same.

Zenneck⁴ has shown how these effective values of inductance capacity and resistance can be computed when the current and voltage distributions are known. Thus, if at any point x on the oscillator, the current i and the voltage v are given by

$$i = I f(x); v = V \phi(x)$$

where I is the value of the current at the current loop and V the maximum voltage, then the differential equation of the oscillation is

$$\frac{\partial I}{\partial t} \int R_1 f(x)^2 dx + \frac{\partial^2 I}{\partial t^2} \int L_1 f(x)^2 dx + \frac{1}{\int C_1 \phi(x) dx} \left\{ \frac{\int C_1 \phi(x) dx}{\int C_1 \phi(x)^2 dx} \right\}^2 = 0$$

where the integrals are taken over the whole oscillator. If we write

$$R_e = \int R_1 f(x)^2 dx \quad (10)$$

$$L_e = \int L_1 f(x)^2 dx \quad (11)$$

$$C_e = \frac{\left\{ \int C_1 \phi(x) dx \right\}^2}{\int C_1 \phi(x)^2 dx} \quad (12)$$

the equation becomes

$$R_e \frac{\partial I}{\partial t} + L_e \frac{\partial^2 I}{\partial t^2} + \frac{I}{C_e} = 0$$

which is the differential equation of oscillation of a simple circuit with lumped resistance, inductance, and capacity of values R_e , L_e , and C_e and in which the current is the same as the maximum in the distributed case. In order to evaluate these quantities, it is necessary only to determine $f(x)$ and $\phi(x)$; that is, the functions which specify the distribution of current and voltage on the oscillator. In this connection it will be assumed that the resistance is not of importance in determining these distributions.

⁴Zenneck, "Wireless Telegraphy" (Translated by A. E. Seeliger, Note 40, p. 410.

At the far end of the aerial the current is zero, that is for $x=l$; $i_l=0$. From equations (3) and (4) for $x=l$

$$v_l = \cos \omega t (A \cos \omega \sqrt{C_1 L_1} l + B \sin \omega \sqrt{C_1 L_1} l)$$

$$i_l = \sin \omega t \sqrt{\frac{C_1}{L_1}} (A \sin \omega \sqrt{C_1 L_1} l - B \cos \omega \sqrt{C_1 L_1} l)$$

and since $i_l=0$

$$A \sin \omega \sqrt{C_1 L_1} l = B \cos \omega \sqrt{C_1 L_1} l$$

From (3) then we obtain

$$r = r_l \cos (\omega \sqrt{C_1 L_1} l - \omega \sqrt{C_1 L_1} x)$$

Hence
$$\phi(x) = \cos (\omega \sqrt{C_1 L_1} l - \omega \sqrt{C_1 L_1} x)$$

Now for $x=0$ from (4) we obtain

$$i_0 = -B \sqrt{\frac{C_1}{L_1}} \sin \omega t = -A \sqrt{\frac{C_1}{L_1}} \tan \omega \sqrt{C_1 L_1} l \sin \omega t$$

whence

$$i = i_0 \frac{\sin (\omega \sqrt{C_1 L_1} l - \omega \sqrt{C_1 L_1} x)}{\sin \omega \sqrt{C_1 L_1} l}$$

and

$$f(x) = \frac{\sin (\omega \sqrt{C_1 L_1} l - \omega \sqrt{C_1 L_1} x)}{\sin \omega \sqrt{C_1 L_1} l}$$

We can now evaluate the expressions (10), (11), and (12). From (10)

$$\begin{aligned} R_c &= \int_0^l R_1 \frac{\sin^2 (\omega \sqrt{C_1 L_1} l - \omega \sqrt{C_1 L_1} x) dx}{\sin^2 \omega \sqrt{C_1 L_1} l} \\ &= \frac{R_1}{\sin^2 \omega \sqrt{C_1 L_1} l} \left[\frac{l}{2} - \frac{\sin 2 \omega \sqrt{C_1 L_1} l}{4 \omega \sqrt{C_1 L_1}} \right] \\ &= \frac{R_1}{2} \left[\frac{1}{\sin^2 \omega \sqrt{C_1 L_1}} - \frac{\cot \omega \sqrt{C_1 L_1}}{\omega \sqrt{C_1 L_1}} \right] \end{aligned} \quad (13)$$

and from (11) which contains the same form of integral

$$L_c = \frac{L_0}{2} \left[\frac{1}{\sin^2 \omega \sqrt{C_0 L_0}} - \frac{\cot \omega \sqrt{C_0 L_0}}{\omega \sqrt{C_0 L_0}} \right] \quad (14)$$

and from (12)

$$\begin{aligned} C_c &= \frac{\int_0^l C_1 \cos^2 (\omega \sqrt{C_1 L_1} l - \omega \sqrt{C_1 L_1} x) dx}{\int_0^l C_1 \cos^2 (\omega \sqrt{C_1 L_1} l - \omega \sqrt{C_1 L_1} x) dx} \\ &= \frac{C_1 \frac{\sin^2 \omega \sqrt{C_1 L_1} l}{(\omega \sqrt{C_1 L_1})^2}}{C_1 \left(\frac{l}{2} + \frac{\sin 2 \omega \sqrt{C_1 L_1} l}{4 \omega \sqrt{C_1 L_1}} \right)} \\ &= \frac{C_0}{\left[\frac{\omega \sqrt{C_0 L_0} \cot \omega \sqrt{C_0 L_0}}{2} + \frac{\omega^2 L_0 C_0}{2 \sin^2 \omega \sqrt{C_0 L_0}} \right]} \end{aligned} \quad (15)$$

The expressions (14) and (15) should lead to the same value for the reactance X of the aerial as obtained before. It is readily shown that

$$X = \omega L_e - \frac{1}{\omega C_e} = -\sqrt{\frac{L_o}{C_o}} \cot \omega \sqrt{C_o L_o}$$

agreeing with equation (6).

It is of interest to investigate the values of these quantities at very low frequencies ($\omega \doteq 0$), frequently called the static values, and those corresponding to the natural frequency of the unloaded antenna or the so-called fundamental of the antenna. Substituting $\omega = 0$ in (13), (14), and (15) and evaluating the indeterminate which enters in the first two cases we obtain for the low frequency values

$$\begin{aligned} R_e &= \frac{R_o}{3} \\ L_e &= \frac{L_o}{3} \\ C_e &= C_o \end{aligned} \tag{16}$$

At low frequencies, the current is a maximum at the lead-in end of the aerial and falls off linearly to zero at the far end. The effective resistance and inductance are one-third of the values which would obtain if the current were the same thruout. The voltage is, however, the same at all points and hence the effective capacity is the capacity per unit length times the length or C_o .

At the fundamental of the antenna, the reactance X of equation (6) becomes equal to zero and hence $\omega \sqrt{C_o L_o} = \frac{\pi}{2}$. Substituting this value in (13), (14), and (15)

$$\left. \begin{aligned} R_e &= \frac{R_o}{2} \\ L_e &= \frac{L_o}{2} \\ C_e &= \frac{8}{\pi^2} C_o \end{aligned} \right\} \tag{17}$$

Hence in going from low frequencies up to that of the fundamental of the antenna, the resistance (neglecting radiation and skin effect) and the inductance (neglecting skin effect) increase by fifty per cent., the capacity, however, decreases by about twenty per cent. The incorrect values $\frac{2}{\pi} L_o$ and $\frac{2}{\pi} C_o$ have been fre-

quently given and commonly used as the values of the effective inductance and capacity of the antenna at its fundamental.

These lead also to the incorrect value $L_e = \frac{L_o}{2}$ for the low frequency inductance⁵.

The values for other frequencies may be obtained by substitution in (13), (14), (15). If the value L of the loading coil in the lead-in is given, the quantity $\omega \sqrt{C_o L_o}$ is directly obtained from Table 1.

4. EQUIVALENT CIRCUIT WITH LUMPED CONSTANTS

Insofar as the frequency or wave length is concerned, the aerial of the antenna may be considered to have constant values of inductance and capacity and the values of frequency or wave length for different loading coils may be computed with slight error using the simple formula applicable to circuits with lumped inductance and capacity. The values of inductance and capacity ascribed to the aerial are the static or low frequency, that is, $\frac{L_o}{3}$ for the inductance and C_o for the capacity. The total inductance in case the loading coil has a value L will be $L + \frac{L_o}{3}$ and the frequency is given by

$$f = \frac{1}{2\pi \sqrt{\left(L + \frac{L_o}{3}\right) C_o}} \quad (18)$$

or the wave length in meters by

$$\lambda = 1884 \sqrt{\left(L + \frac{L_o}{3}\right) C_o} \quad (19)$$

where the inductance is expressed in microhenrys and the capacity in microfarads. The accuracy with which this formula gives the wave length can be determined by comparison with the exact formula (8). In the second column of Table I are given

⁵These values are given by J. H. Morecroft in "Proc. I. R. E." 5, p. 389, 1917. It may be shown that they lead to correct values for the reactance of the aerial and hence to correct values of frequency as was verified by the experiments. They are not, however, the values which would be correct for an artificial antenna in which the current must equal the maximum in the actual antenna and in which the energies must also be equal to those in the antenna. The resistance values given by Prof. Morecroft agree with these requirements and with the values obtained here.

Values for the effective inductance and capacity in agreement with those of equation (17) above have been given by G. W. O. Howe, "Yearbook of Wireless Telegraphy and Telephony," page 699, 1917.

the values of $\omega\sqrt{C_o L_o}$ for different values of L_o as computed by formula (8). Formula (18) may be written in the form

$$\omega\sqrt{L_o C_o} = \frac{1}{\sqrt{\frac{L}{L_o} + \frac{1}{3}}}$$

so that the values of $\omega\sqrt{C_o L_o}$, which are proportional to the frequency, may readily be computed from this formula also. These values are given in the third column of Table I and the per cent. difference in the fourth column. It is seen that formula (18) gives values for the frequency which are correct to less than a per cent., excepting when very close to the fundamental of the antenna, i. e., for very small values of L . Under these conditions the simple formula leads to values of the frequency which are too high. Hence to the degree of accuracy shown, which is amply sufficient in most practical cases, *the aerial can be represented by its static inductance $\frac{L_o}{3}$ with its static capacity C_o in series, and the frequency of oscillation with a loading coil L in the lead-in can be computed by the ordinary formula applicable to circuits with lumped constants.*

In an article by L. Cohen,⁶ which has been copied in several other publications, it was stated that the use of the simple wave length formula would lead to very large errors when applied to the antenna with distributed constants. The large errors found by Cohen are due to his having used the value L_o for the inductance of the aerial, instead of $\frac{L_o}{3}$, in applying the simple formula.

IV. THE INDUCTANCE COIL

The transmission line theory can also be applied to the treatment of the effects of distributed capacity in inductance coils. In Figure 7 (a) is represented a single layer solenoid connected to a variable condenser C . A and B are the terminals of the coil, D the middle, and the condensers drawn in dotted lines are supposed to represent the capacities between the different parts of the coil. In Figure 7 (b) the same coil is represented as a line with uniformly distributed inductance and capacity. These assumptions are admittedly rough, but are somewhat justified by the known similarity of the oscillations in long solenoids to those in a simple antenna.

⁶ See foot-note 3.

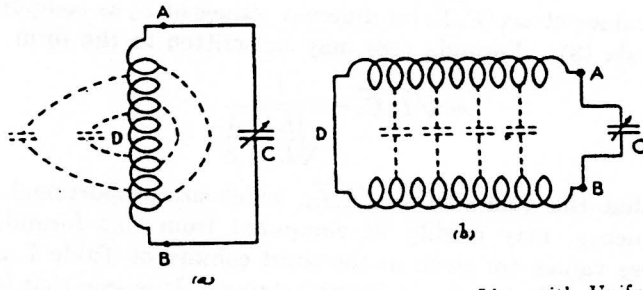


FIGURE 7—Inductance Coil Represented as a Line with Uniform Distribution of Inductance and Capacity

1. REACTANCE OF THE COIL

Using the same notation as before, an expression for the reactance of the coil, regarded from the terminals $A B$ ($x=0$), will be determined considering the line as closed at the far end D ($x=l$). Equations (3) and (4) will again be applied, taking account of the new terminal condition, that is, for $x=l$; $v=0$. Hence

$$A \cos \omega \sqrt{C_1 L_1} l = -B \sin \omega \sqrt{C_1 L_1} l$$

and for $x=0$

$$v_o = A \cos \omega t = -B \tan \omega \sqrt{C_1 L_1} l \cos \omega t$$

$$i_o = -\sqrt{\frac{C_1}{L_1}} B \sin \omega t$$

which gives for the reactance of the coil regarded from the terminals $A B$,

$$X' = \sqrt{\frac{L_1}{C_1}} \tan \omega \sqrt{C_1 L_1} l$$

or

$$X' = \sqrt{\frac{L_o}{C_o}} \tan \omega \sqrt{C_o L_o} \quad (20)$$

2. NATURAL FREQUENCIES OF OSCILLATION

At low frequencies, the reactance of the coil is very small and positive, but increases with increasing frequency and becomes infinite when $\omega \sqrt{C_o L_o} = \frac{\pi}{2}$. This represents the lowest frequency of natural oscillation of the coil when the terminals are open. Above this frequency the reactance is highly negative, approaching zero at the frequency $\omega \sqrt{C_o L_o} = \pi$. In this range of frequencies, the coil behaves as a condenser and would require

an inductance across the terminals to form a resonant circuit. At the frequency $\omega \sqrt{C_o L_o} = \pi$ the coil will oscillate with its terminals short-circuited. As the frequency is still further increased the reactance again becomes increasingly positive.

(a) CONDENSER ACROSS THE TERMINALS. The natural frequencies of oscillation of the coil when connected to a condenser C are given by the condition that the total reactance of the circuit shall be zero.

$$X' + X_c = 0$$

From this we have

$$\sqrt{\frac{L_o}{C_o}} \tan \omega \sqrt{C_o L_o} = \frac{1}{\omega C}$$

or

$$\frac{\cot \omega \sqrt{C_o L_o}}{\omega \sqrt{C_o L_o}} = \frac{C}{C_o} \quad (21)$$

This expression is the same as (8) obtained in the case of the loaded antenna, excepting that $\frac{C}{C_o}$ occurs on the right-hand side instead of $\frac{L}{L_o}$, and shows that the frequency is decreased and wave length increased by increasing the capacity across the coil in a manner entirely similar to the decrease in frequency produced by inserting loading coils in the antenna lead-in.

3. EQUIVALENT CIRCUIT WITH LUMPED CONSTANTS

It is of interest to investigate the effective values of inductance and capacity of the coil at very low frequencies. Expanding the tangent in equation (20) into a series we find

$$X' = \omega L_o \left(1 + \frac{\omega^2 C_o L_o}{3} + \dots \right)$$

and neglecting higher power terms this may be written

$$X' = \frac{(\omega L_o) \left(-\frac{3}{\omega C_o} \right)}{\omega L_o - \frac{3}{\omega C_o}}$$

This is the reactance of an inductance L_o in parallel with a capacity $\frac{C_o}{3}$ which shows that at low frequencies the coil may be regarded as an inductance L_o with a capacity $\frac{C_o}{3}$ across the terminals and, therefore, in parallel with the external condenser

FURTHER DISCUSSION* ON
"ELECTRICAL OSCILLATIONS IN ANTENNAS AND
INDUCTION COILS" BY JOHN M. MILLER

By
JOHN H. MORECROFT

I was glad to see an article by Dr. Miller on the subject of oscillations in coils and antennas because of my own interest in the subject, and also because of the able manner in which Dr. Miller handles material of this kind. The paper is well worth studying.

I was somewhat startled, however, to find out from the author that I was in error in some of the material presented in my paper in the PROCEEDINGS OF THE INSTITUTE OF RADIO ENGINEERS for December, 1917, especially as I had at the time I wrote my paper thought along similar lines as does Dr. Miller in his treatment of the subject; this is shown by my treatment of the antenna resistance.

As to what the effective inductance and capacity of an antenna are when it is oscillating in its fundamental mode is, it seems to me, a matter of viewpoint. Dr. Miller concedes that my treatment leads to correct predictions of the behavior of the antenna and I concede the same to him; it is a question, therefore, as to which treatment is the more logical.

From the author's deductions we must conclude that at quarter wave length oscillations

$$L_e = \frac{L_o}{2} \quad (1)$$

$$C_e = \frac{8}{\pi^2} C_o \quad (2)$$

The value of L really comes from a consideration of the magnetic energy in the antenna keeping the current in the artificial antenna the same as the maximum value it had in the actual antenna, and then selecting the capacity of suitable value to give the artificial antenna the same natural period as the actual antenna. This method of procedure will, as the author states, give an artificial antenna having the same natural frequency, magnetic energy, and electrostatic energy, as the actual antenna, keeping the current in the artificial antenna the same as the maximum current in the actual antenna.

* Received by the Editor, June 26, 1919.

But suppose he had attacked the problem from the viewpoint of electrostatic energy instead of electromagnetic energy, and that he had obtained the constants of his artificial antenna to satisfy these conditions (which are just as fundamental and reasonable as those he did satisfy); same natural frequency, same magnetic energy, same electrostatic energy and the same voltage across the condenser of the artificial as the maximum voltage in the actual antenna. He would then have obtained the relations

$$L_a = \frac{8}{\pi^2} L_n \quad (3)$$

and

$$C_a = \frac{C_n}{2} \quad (4)$$

Now equations (3) and (4) are just as correct as are (1) and (2) and moreover the artificial antenna built with the constants given in (3) and (4) would duplicate the actual antenna just as well as the one built according to the relations given in (1) and (2).

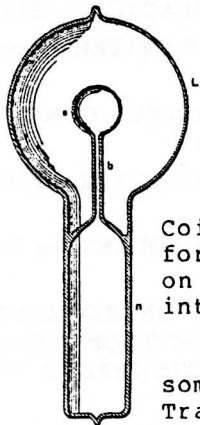
I had these two possibilities in mind when writing in my original article "as the electrostatic energy is a function of the potential curve and the magnetic energy is the same function of the current curve, and both these curves have the same shape, it is logical, *and so on.*" Needless to say, I still consider it logical, and after reading this discussion I am sure Dr. Miller will see my reasons for so thinking.

When applying the theory of uniform lines to coils I think a very large error is made at once, which vitiates very largely any conclusions reached. The L and C of the coil, per centimeter length, are by no means uniform, a necessary condition in the theory of uniform lines; in a long solenoid the L per centimeter near the center of the coil is nearly twice as great as the L per centimeter at the ends, a fact which follows from elementary theory, and one which has been verified in our laboratory by measuring the wave length of a high frequency wave traveling along such a solenoid. The wave length is much shorter in the center of the coil than it is near the ends. What the capacity per centimeter of a solenoid is has never been measured, I think, but it is undoubtedly greater in the center of the coil than near the ends.

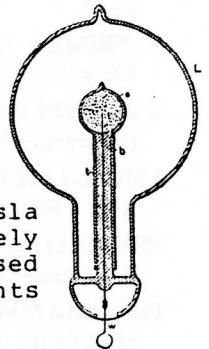
The conclusions he reaches from his equation (22) that even at its natural frequency the L of the coil may be regarded as equal to the low frequency value of L is valuable in so far as it enables one better to predict the behavior of the coil, but it

should be kept in mind that really the value of L of the coil, when defined as does the author in the first part of his paper in terms of magnetic energy and maximum current in the coil, at the high frequency, is very much less than it is at the low frequency.

One point on which I differ very materially with the author is the question of the reactance of a coil and condenser, connected in parallel, and excited by a frequency the same as the natural frequency of the circuit. The author gives the reactance as infinity at this frequency, whereas it is actually zero. When the impressed frequency is slightly higher than resonant frequency there is a high capacitive reaction and at a frequency slightly lower than resonant frequency there is a high inductive reaction, but at the resonant frequency the reactance of the circuit is zero. The resistance of the circuit becomes infinite at this frequency, if the coil and condenser have no resistance, but for any value of coil resistance, the reactance of the combination is zero at resonant frequency.



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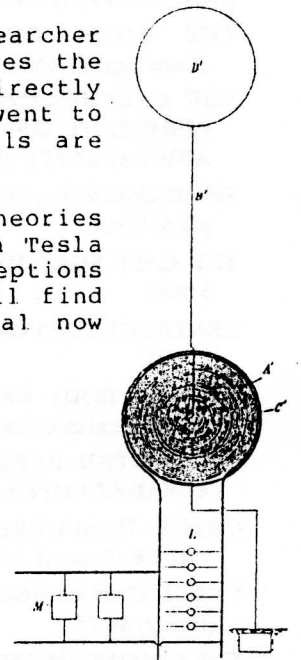
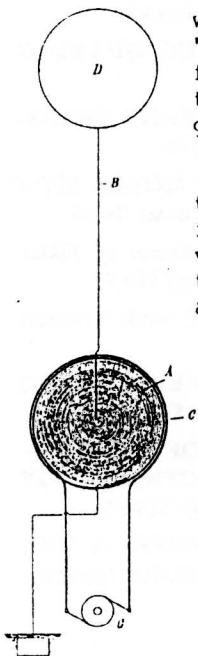
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